

1) If $2^x = 4$ is given, work out $\frac{8^x}{4} + \frac{32^x}{64}$

如果 $2^x = 4$, 計算出 $\frac{8^x}{4} + \frac{32^x}{64}$

- A) 48 B) 64
C) 33 D) 32

2) Solve this equation 解這個方程

$$\frac{1}{x+1} - \frac{5}{x-1} = \frac{2}{x^2-1}$$

- A) -2 B) 1
C) 3 D) 2,5

2) How many elements of the set $\{1, 2, 3, \dots, 61\}$ divisible by 4 or 7 ?
集合 $\{1, 2, 3, \dots, 61\}$ 中有多少元素可以被 4 或 7 整除 ?

- A) 14 B) 21
C) 22 D) 30

3) Assuming $a \neq 5, b \neq 6$, and $c \neq 7$, what is the value in the simplest form of the following expression?

假設 $a \neq 5$, $b \neq 6$ 和 $c \neq 7$, 以下表達式的最簡單形式的值是多少 ?

$$\frac{a-3}{7-c} \cdot \frac{b-6}{3-a} \cdot \frac{c-7}{6-b}$$

- A) 1 B) $\frac{abc}{60}$
C) -1 D) a

5) The sum of the digits of n is written

$S(n)$. For example

$$S(7) = 7 \text{ and } S(2024) = 2 + 0 + 2 + 4 = 8$$

n 的數字之和記為 $S(n)$ 。例如

$$S(7)=7 \text{ 和 } S(2024)=2+0+2+4=8$$

This notation can be written multiple times for example

$$S(S(59)) = S(5 + 9) = S(14) = 1 + 4 = 5$$

Which of the following has $S((n)) = 9$

例如，這個符號可以寫多次

$$S(S(59))=S(5+9)=S(14)=1+4=5$$

下列哪項的 $S((n))=9$

- A) 1534 B) 1857
C) 1898 D) 1962

6) What is the 2023rd letter in this sequence?

這個序列中的第2023rd 個字母是什麼 ?
AMCEFCMAAMCEFCMAAMCEFCMAA
MCEFCMA

- A) A B) E
C) C D) M

7) Solve 求解: $4^3 - 3^2 + 5^3 + 8^2 = ?$

- A) 244 B) 444
C) 458 D) 284

8) What is the value of 值是多少

$$9,000,000 - 900,000 + 9,000 - 900 + 90 - 9 = ?$$

A) 8108181

C) 818181

B) 8181081

D) 8181810

9) Find 找出 $\sqrt{2} \times a = ?$

$$\frac{1 + \frac{1}{a}}{a+1}$$

$$1 + a + \frac{\frac{1}{a}}{1-a} = 4$$

A) 1

B) $\sqrt{2}$

C) $\sqrt{3}$

D) 2

10) Find the value of $y + z - x = ?$

求 $y + z - x = ?$

$$\left. \begin{array}{l} xy = z + 4 \\ zx = y + 6 \\ z = 5 - y \end{array} \right\}$$

A) 4

B) 0.5

C) 3

D) 2

11) Solve 求解:

$$\log_6 12 = x \Rightarrow \log_{12} 24 = ?$$

A) $\frac{2x-1}{x+1}$

C) $\frac{2x-1}{x}$

B) 1

D) $\frac{x-2}{x}$

12) Find the value of $A \times B = ?$

求 $A \times B = ?$

$$A = \frac{3}{3 + \frac{1}{7}}, \quad B = \frac{3}{1-A}$$

A) 42

C) 63

B) 52

D) 66

13) Simplify: 簡化:

$$\frac{a^2b - 3a^2 - 3a + ab - 2b + 6}{ab^2 + 2b^2 - 10b - 5ab + 6a + 12} + \frac{1}{b-2} = ?$$

A) $\frac{a-1}{b-2}$

C) $\frac{1}{b+2}$

B) $\frac{a}{b-2}$

D) a

14) Find the value of $\frac{3A}{\sqrt{5}} = ?$

求出 $\frac{3A}{\sqrt{5}} = ?$

$$A = \frac{\sqrt{15}}{3} - \sqrt{9 - \frac{1}{9}} + \frac{\sqrt{405}}{27}$$

A) $\sqrt{3} - 3$

C) $\sqrt{3} - 1$

B) $1 - \sqrt{3}$

D) $2\sqrt{3}$

15) Find the value of $2x + y - 2z = ?$

求出 $2x + y - 2z = ?$

$$\left. \begin{array}{l} x + 2y + 3z = 7 \\ x + 3y = 5 \\ 3y + 4z = 7 \end{array} \right\}$$

A) 4

C) 3

B) 0

D) 6

16) Simplify: 簡化 :

$$\frac{\cos x}{1 + \sin x} + \tan x = ?$$

A) $\cos x$

B) $\cot x$

$$\frac{1}{\cos x}$$

C) $\sin x$

D) $\cos x$

17) Find the value of $A+B+C+D=?$

找 $A+B+C+D=$ 的值

$$\begin{array}{r} \begin{array}{rrr} \textbf{A} & \textbf{B} & \textbf{C} \\ + & \textbf{B} & 8 & \textbf{D} \end{array} & \quad & \begin{array}{r} 8 & \textbf{B} & \textbf{D} \\ - & \textbf{A} & \textbf{C} & \textbf{B} \end{array} \\ \hline \begin{array}{rrr} 8 & \textbf{D} & 0 \end{array} & \quad & \begin{array}{rrr} \textbf{B} & \textbf{B} & 9 \end{array} \end{array}$$

A) 16

B) 17

C) 18

D) 20

18) What is the next number?

下一個數字是多少？

2, 5, 10, 17, 26, 37, ...

A) 45

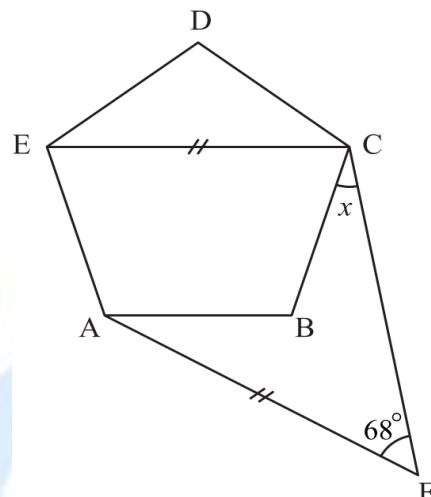
B) 50

C) 53

D) 49

19) ABCDE is a regular pentagon,

ABCDE是正五邊形，



$$|EC| = |AF|$$

$$m(\widehat{AFC}) = 68^\circ$$

$$m(\widehat{BCF}) = x = ?$$

A) 30

B) 32

C) 40

D) 36

20) Solve: 求解:

$$\left(\frac{2}{\sqrt{3}-1} + \frac{3}{\sqrt{3}-2} + \frac{15}{3-\sqrt{3}} \right) \cdot (2\sqrt{3} + 10)^{-1} = ?$$

A) 4

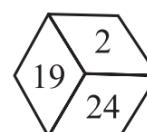
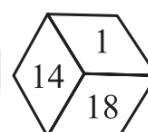
B) 1

C) $\frac{1}{2}$

D) $\frac{1}{4}$

21) Find the missing number.

找丢失的號碼。



Answer 答案: _____

22) Find the greatest value of x.

找x的最大值。

$$\left(\frac{x+3}{x-1}\right)^2 + 12 = 64 \left(\frac{x-1}{x+3}\right)^2$$

Answer 答案: _____

23) Solve: 求解:

$$\begin{array}{rcl} \text{舌头伸出} & + & \text{舌头伸出} & + & \text{舌头伸出} = 33 \\ \text{舌头伸出} & + & \text{哭泣} & + & \text{哭泣} = 17 \\ \text{哭泣} & + & \text{哭泣} & + & \text{闭眼} = 13 \\ \text{闭眼} & \times & \text{哭泣} & + & \text{舌头伸出} = ? \end{array}$$

Answer 答案: _____

24) Evaluate 求解:

$$2\left(1 + \frac{1}{2}\right) + 3\left(1 + \frac{1}{3}\right) + 4\left(1 + \frac{1}{4}\right) + \cdots + 20\left(1 + \frac{1}{20}\right) = ?$$

Answer 答案: _____

25) Let d and e denote the solution of $4x^2 + 15x - 4 = 0$. What is the value of $4(d-1)(e-1) = ?$

假設d和e表示 $4x^2 + 15x - 4 = 0$ $4(d-1)(e-1) = ?$ 的值是多少？

Answer 答案: _____